

Calculation Policy

Brize Norton Primary School

We SHINE for ourselves and each other with kindness.

Strive, Help, Inspire, Nurture, Excel

Adopted by school LGB:	Brize Norton Primary School
Date:	March 2026
Review Date:	March 2029

	EYFS	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Counting	Counting forwards and backwards in 1 s to and beyond 10. Counting forwards and backwards in 10s to one hundred Begin to count in 5s and 2s forwards and backwards (if able)	Counting in 1s on and back to 100 with then without a hundred square Counting on and back in 10s from any number to one hundred with then without a hundred square. Counting forwards and backwards in 2s 5s and 10s from 0.	Counting forwards and backwards in 10s and 1s to 100 and over (practice crossing 100 boundary) Counting forwards and backwards in 2s 5s and 10s from any number (not always starting at 0) Begin to count in 3s from 0 (with then without a hundred square)	Counting forwards and backwards in 1s, 10s, 100s from any 2 or 3 digit number crossing 1000 boundary. Counting forwards and backwards in 2s 5s crossing 100 boundaries and from any number. Counting forwards and backwards in in 3s, 4s and 8s from any number to 100 (with then without hundred square) Count forwards and backwards in	Counting forwards and backwards in 10s, 100s, 1000s from any 3 or 4 digit number crossing 10,000 boundaries. Counting in tenths and hundredths crossing units boundary. (Use hundred square, bead string and coins, decimal and fraction cards.) Counting forwards and backwards in multiples of 6, 7, 9, 11, 12	Counting in all powers of 10 crossing boundaries up to 1 million. Counting in tenths, hundredths crossing boundaries. (Use hundred square, bead string and coins, decimal, fraction cards and percentage.) Counting in thousandths crossing boundaries. Counting in positive and negative numbers	Counting in all powers of 10 crossing boundaries up to 10 million. Counting in tenths, hundredths and thousandths crossing boundaries. Use negative numbers in context and calculate intervals across 0.

				50s and 100s. Make links between multiples of 2, 4, 8. Count up and down in tenths seeing decimals notation. Use money. (10ps 0.10)	Make links between multiples of 3, 6, 12 and 2, 4, 8 Count in multiples of 25 relate to quarters. Count backwards through zero into negative numbers		
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Addition	Exploring numbers to 5 in practical contexts. Recognising a number on my fingers/dice. Beginning to recall number facts of all numbers to 5 For example $2+3=5$ $1+4=5$ $2+2=4$	Starting at the bigger number and counting on using number line/cubes and fingers. Learning addition facts of all numbers to 10 (e.g. $3+4=7$) Relate addition facts to 10 to those to 20. $4 + 6 = 10$ $14 + 6 = 20$ Begin to learn by heart addition facts which cross 10 e.g. $4 + 7 = 11$ Say 1 more than a given number	Adding three single digits (using known pairs) Adding 9 or 11 using ten and adjust. Using known number facts to 10 to calculate number facts to 20 e.g. $12+6$ Learning by heart facts which bridge 10. E.g. $5+7$	Continue to practice number facts which bridge 10 e.g. $8+5$ Link to multiples of 10 e.g. $80+50$ Continue adding 9 or 11 using 10 and adjusting. Extend to adding 29 or 31 by adding nearest multiple of 10 and adjusting. Mental addition of 2 digit numbers (abstract) Mental addition of multiples of 100s 10s or 1 to any 3 digit number. Recognise pairs of multiples of 100 with a total of 1000	Practice adding multiples of 10, 100 and 1000 using number bonds as base facts. (focus on crossing boundaries) Find 1000 more than any given number. Practice mental addition from Year 3- partitioning, using near multiples e.g. $+59$ by adding $60 - 1$ Add 91 by adding 90 and then add 1.	Practice adding powers of 10 using number bonds and place value facts., Add easy 2 and 3 digit numbers fluently. Add fractions where denominators are the same.	Practice adding powers of 10 using number bonds and place value facts., Use place value and number facts to solve problems in algebraic form.
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				Recognise pairs of multiples of 5 with a total of 100			
Subtraction	Beginning to recall facts for numbers to 5 $5-3=2$ $4-2=2$ Counting up to find a small difference to 5 or 10 (if able) Find one less than numbers to 20.	Starting at the bigger number and counting back using number line/cubes and fingers. Learning subtraction facts of all numbers to 10 (e.g. $3+4=7$) Relate subtraction facts to 10 to those to 20. $4+6=10$ $14+6=20$ Begin to learn by heart subtraction facts which cross 10 e.g. $11+4=7$ Say 1 less than a given number and Counting up to find a small difference in	Subtracting 9 or 11 using ten and adjust. Continue to learn and practice number facts to 10 to and 20 calculate number facts to 20 e.g. $12-8=$ Learning by heart facts which bridge 10. E.g. $12-5=7$ Count up to find a small difference in numbers to 100	Continue to practice subtraction facts which bridge 10 e.g. $8+5$ Link to multiples of 10 e.g. $80+50$ Continue subtract 9 or 11 using 10 and adjusting. Extend to subtracting 29 or 31 by adding nearest multiple of 10 and adjusting. Mental subtract of 2 digit numbers (abstract) Mental subtraction of multiples of 100s 10s or 1 to any 3 digit number. Count up to find small differences	Practice subtracting multiples of 10, 100 and 1000 using number bonds as base facts. (focus on crossing boundaries) Find 1000 less than any given number. Practice mental subtraction from Year 3- partitioning, using near multiples e.g. -59 by subtracting $60+1$ Subtract 91 by Subtracting 90 and then subtracting 1. Count up to find small differences	Practice subtracting powers of 10 using number bonds and place value facts. Subtract easy 2 and 3 digit numbers fluently. Subtract fractions where denominators are the same. Practice mental subtraction from Year 3 and 4- partitioning, using near multiples e.g. -559 by subtracting $560+1$ Subtract 901 by Subtracting 900 and then subtracting 1.	Practice subtracting powers of 10 using number bonds and place value facts., Use place value and number facts to solve problems in algebraic form

		numbers to 10 then 50 and 100		in numbers to 1000	in numbers to 10,000	Count up to find small differences in numbers to 1 million	
Multiplication	Begin to learn by heart some doubles if able e.g. double 2 is 4	Know by heart doubles of all numbers to at least 10 + 10 Begin to learn 10x table facts and link to counting in 10s	Learn 2x 5 x10 tables spend at least a term learning each one (1 at a time) Practice doubles to 20 including those which require partitioning e.g. 14+14=	Learn 3x, 4x, 8x tables. Continue to practice 2x 5 x 10. Practice multiplying a number by 10 using practical resources (place value grids) Use times table facts and place value to multiply multiples of 10 and 100 e.g 2x 5 = 2x 50 = 100	Learn 6x 7x 9x 11x 12x tables by heart (spend a term learning each one) Continue to practice the rest of the tables. Multiply numbers by 10 and 100 using place value grids. Include decimals to 1 place. Use times table facts and place value to multiply multiples of 10 and 100 e.g. Use chains: 2 x 0.5 = 1 2x 5 = 10 2x 50 = 100 2x 500 = 1,000 2 x 5000 = 10, 000	Apply all multiplication tables to 12 x 12 to calculating with powers of 10 and decimals. Multiply numbers by 10, 100 and 1000 including to decimals with 3 decimal places	Apply all multiplication tables to 12 x 12 to calculating with powers of 10 and decimals. Multiply numbers by 10, 100 and 1000 including to decimals with 3 decimal places Use place value and number facts to solve problems in algebraic form

Division		Halve even numbers to 20. Begin to learn 10x table division facts and link to counting in 10s.	Practice division facts for 2x 5x 10x tables relating to multiplication and fractions. Know halves of all numbers to 20.	Relate division facts for 3x 4x 8x to multiplication facts. Continue to practice division facts for 2x 5x 10. Practice dividing a number by 10 using practical resources (place value grids)	Practice division facts for 6x 7x 9x 11x 12 alongside learning multiplication facts and link to fractions. Divide numbers by 10 and 100 using place value grids. Include decimals to 1 place. Use times table facts and place value to multiply multiples of 10 and 100 e.g. Use chains: $1 \div 2 = 0.5$ $10 \div 2 = 5$ $100 \div 2 = 50$ $1000 \div 2 = 500$ $10,000 \div 2 = 5000$	Use the rapid recall of table and division facts to 12 x 12 to identify prime numbers to 100. Divide numbers by 10, 100 and 1000 including to decimals with 3 decimal places. Apply knowledge of table facts and place value to divide multiples of 10, 100, 1000, 10,000, 100,000 e.g. $500,000 \div 50 =$	Use the rapid recall of table and division facts to 12 x 12 to identify prime numbers to 100. Divide numbers by 10, 100 and 1000 including to decimals with 3 decimal places. Apply knowledge of table facts and place value to divide multiples of 10, 100, 1000, 10,000, 100,000 e.g. $500,000 \div 50 =$ Use place value and number facts to solve problems in algebraic form.
Rounding	Exploring on number tracks/lines is 6 closer to 10?	Practice number boundaries 16 lies between 10 and 20. Say hello to the next 10 or the 10 before..	Practice number boundaries 23 lies between 20 and 30.	Practice number boundaries. 130 lies between 100 and 200. 23 lies between 20 and 30.	Round numbers to the nearest 10 and 100 and 1000 Practice number boundaries 4500	Round numbers to the nearest 10, 100, 1000, 10,000 and 100,000 Practice number	Round any number to the nearest required degree of accuracy.

					lies between 4000 and 5000 4550 lies between 4500 and 4600	boundaries 45000 lies between 40000 and 50000 45500 lies between 45000 and 46000	
Properties of number	Use correct mathematical language at all times when describing number. Larger, smaller, ones etc	Identify multiples of 10.	Use terms multiples and factors alongside learning times tables.	Use terms multiples and factors alongside learning times tables.	Use terms multiples and factors alongside learning times tables	Use terms multiples and factors alongside learning times tables. Learn square numbers Learn cube numbers Recall prime numbers to 19 and identify to 100 Identify multiples of factors, including factor pairs, prime factors and common factors of two numbers	Identify common factors, common multiples and prime numbers
Fractions, decimals and percentag			Find $\frac{1}{10}$, $\frac{1}{5}$ 1,2 of numbers relating to times tables	Find $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{8}$ of numbers relating to times tables. Begin to add decimals with 1 digit using place	Find unit fractions of numbers based on the times tables they are practicing. Add	Begin to know equivalence of basic fractions, decimals and percentages. 10% 25% 50%	Know equivalence of basic fractions to decimals and percentages 10 % 25% 50% 75%

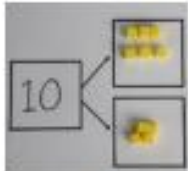
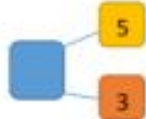
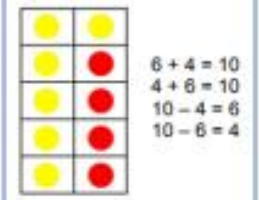
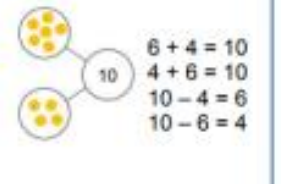
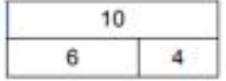
				value (no crossing boundaries) use number facts.	and subtract numbers with 1 decimal place mentally	75% $\frac{1}{4}$ $\frac{1}{3}$ $\frac{1}{5}$ $\frac{1}{10}$ $\frac{1}{100}$ $\frac{1}{1000}$ Mentally add simple decimals to 1 and 2 places.	$\frac{1}{4}$ $\frac{1}{3}$ $\frac{1}{5}$ $\frac{1}{10}$ $\frac{1}{100}$ $\frac{1}{1000}$ Mentally add simple decimals to 1,2 and 3 places.
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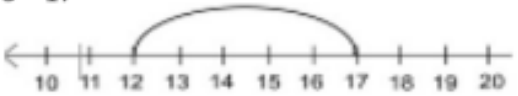
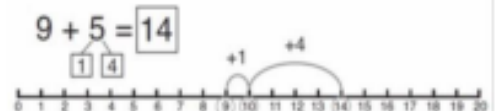
Addition

Addition- EYFS

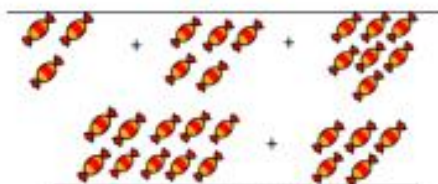
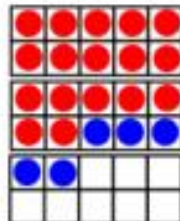
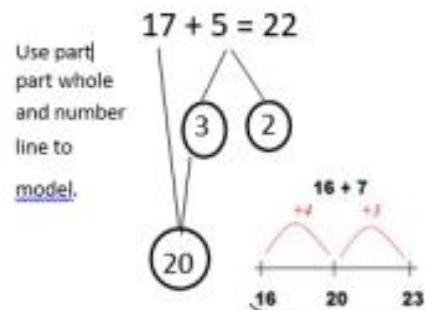
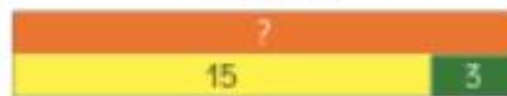
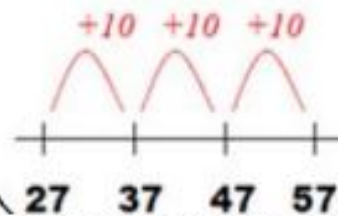
Objectives	Concrete	Pictorial	Abstract												
- Knows that a group of things change in quantity when something is added. - Find the total number of items in two groups by counting all of them. - Says the number that is one more than a given number. - Finds one more from a group of up to five objects, then ten objects. - In practical activities and discussion, beginning to use the vocabulary involved in adding. - Using quantities and objects, they add two single digit numbers and count on to find the answer. - Solve problems including doubling.	Use toys and general classroom resources for children to physically manipulate, group/regroup. Use specific maths resources such as counters, snap cubes, Numicon etc. Use visual supports such as ten frames, part part whole and addition mats, with the physical objects and resources that can be manipulated.	Two groups of pictures so children are able to count the total. Bar model using visuals, pictures/icons or colours. Use visual supports such as ten frames, part part whole and addition mats with pictures/icons.	A focus on symbols and numbers to form a calculation. $5 + 2 = 7$ whole 5, part 3, part 2 <table border="1"> <tr> <td>2</td><td>3</td><td>4</td><td>5</td> </tr> <tr> <td>5</td><td>4</td><td>2</td><td>3</td> </tr> <tr> <td>5</td><td>5</td><td>6</td><td>4</td> </tr> </table> * No expectation for children to be able to record a number sentence/addition calculation.	2	3	4	5	5	4	2	3	5	5	6	4
2	3	4	5												
5	4	2	3												
5	5	6	4												

Addition- Year 1

Objective and Strategy	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part- whole model	 Use cubes to add two numbers together as a group or in a bar. (Some children may still need to use real objects)  Use part-part whole model	 Use pictures to add two numbers together as a group or in a bar. The Bar Model will be continued from EYFS as a method to support problem solving involving addition, continuing with the concrete representations and moving onto using pictorial representations of objects. Some children will also move onto the abstract.  Pictorial (concrete) Abstract	 Use the part-part whole diagram as shown above to move into the abstract. $4 + 3 = 7$ $10 = 6 + 4$
Represent and use number bonds and related subtraction facts within 20	 6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4 Tens Frame (Some children may need to initially use real objects then move onto the representation, egg boxes may also be used to support this)	 6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4 Part Whole Model	 6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4 Bar Model Bar model and part-part whole to be used alongside abstract
Addition and subtraction of one-digit and two-digit numbers to 20 including 0.		$6 + 3 = 9$  Start at the larger number on the number line and count on in ones.	$5 + 12 = 17$ $17 = 12 + 5$

Start at the bigger number and counting on	Start with the larger number on the bead string and then count of to the smaller number 1 by 1 to find the answer.	$12 + 5 = 17$  Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10 (The 'Make 10' strategy)	$6 + 5 = 11$   Start with the bigger number and use the smaller number to make 10. Use ten frames.	$3 + 9 =$  Use pictures or a number line. Regroup or Partition the smaller number using the part part whole model to make 10. $9 + 5 = 14$ 	$7 + 4 = 11$ If I am at seven, how many more do I need to make 10. How many more do I add on now?
Vocabulary	add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, balancing, part, part, whole		

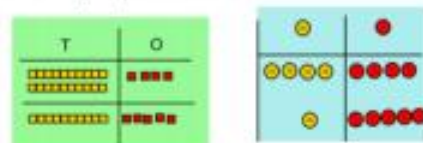
Addition- Year 2

Objective and Strategy	Concrete	Pictorial	Abstract			
Adding 3 1-digit numbers	$4 + 7 + 6 = 17$ Put 4 and 6 together to make 10. Add on 7.  Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	 Add together three groups of objects. Draw a picture to recombine the groups to make 10.	$4 + 7 + 6 = 10 + 7$ $= 17$ Combine the two numbers that make 10 and then add on the remainder.			
Adding a 2-digit number and ones	 $17 + 5 = 22$ Use ten frame to make 'magic ten' Children explore the pattern. $17 + 5 = 22$ $27 + 5 = 32$	Use part part whole and number line to model. $17 + 5 = 22$  Bar Model 	$17 + 5 = 22$ Explore related facts $17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $22 - 5 = 17$ <table border="1" data-bbox="1854 676 2067 754"><tr><td>22</td></tr><tr><td>17</td><td>5</td></tr></table>	22	17	5
22						
17	5					
Adding a 2-digit number and multiples of 10	 $25 + 10 = 35$ Explore that the ones digit does not change	$27 + 30$  Base 10 may be used above the number line initially. The calculation will be shown alongside the number line to see the connection	$27 + 10 = 37$ $27 + 20 = 47$ $27 + 30 = 57$			

Adding two 2-digit numbers (No re-grouping)

$$24 + 15 =$$

Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.

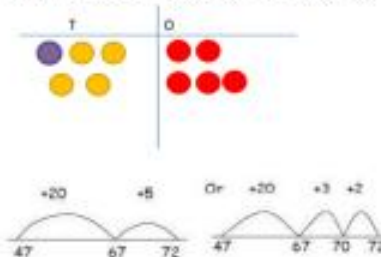


(Some children may not be ready for place value counters in Y2)

Numicon may also be used



After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.



Use number line and bridge ten using part whole if necessary.
Base 10 may be used above the number line.

The calculation will be shown alongside the number line to see the connection

Model	Calculation

The Bar Model (Singapore maths) will be used to support problem solving moving onto the generalisation that $b+c=a$. Children will focus on using the abstract representation with the pictorial to support where necessary.

Partitioning:

$$\begin{array}{r} 25 + 47 \\ \hline 20 + 40 = 60 \\ 5 + 7 = 12 \\ 60 + 12 = 72 \end{array}$$

Recording addition in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method:

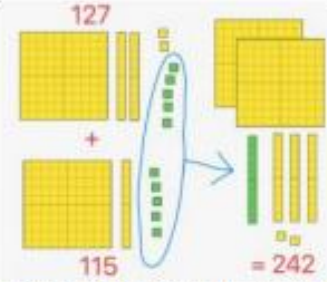
$$\begin{array}{r} 40 + 7 \\ 30 + 5 \\ \hline 70 + 12 \end{array}$$

Vocabulary

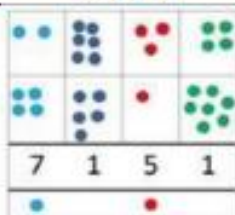
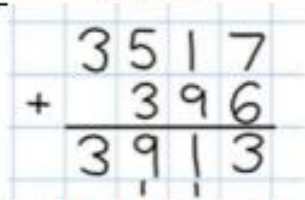
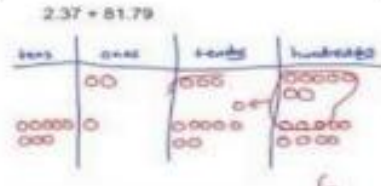
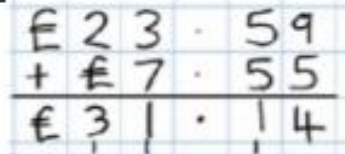
add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

Addition- Year 3

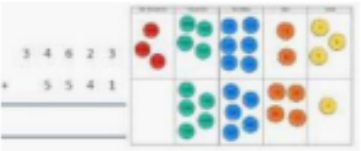
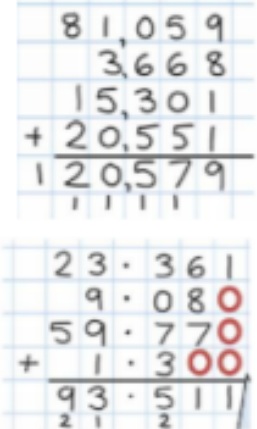
Objective and Strategy	Concrete	Pictorial	Abstract
Add and subtract numbers with up to 3-digits, using formal written methods of columnar addition Column addition (no regrouping)	T O </		

	 Exchange ten ones for a ten. Model using Dienes, Numicon and place value counters.			$\begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$
Vocabulary	addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary			

Addition- Year 4

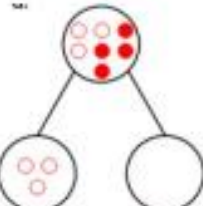
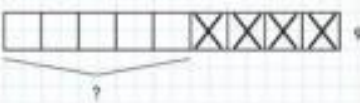
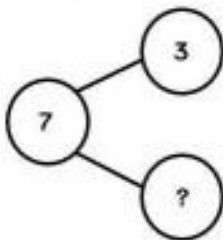
Objective and Strategy	Concrete	Pictorial	Abstract				
Using formal written methods of columnar addition where appropriate add numbers with up to 4 digits (with exchange)	Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand.  The calculation will be shown alongside the manipulative used to see the connection <table><tr><th>Model</th><th>Calculation</th></tr><tr><td></td><td></td></tr></table>	Model	Calculation			 Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.	 Continue from previous work to carry hundreds as well as tens.
Model	Calculation						
Add decimals with 2 decimal places, including money.	 Introduce decimal place value counters and model exchange for addition.		 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.				
Vocabulary	addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal point						

Addition- Year 5/6

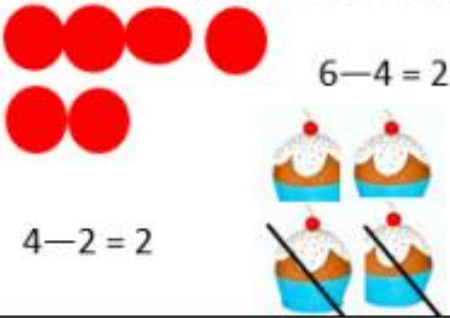
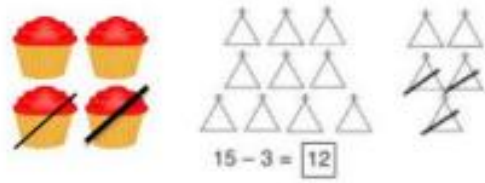
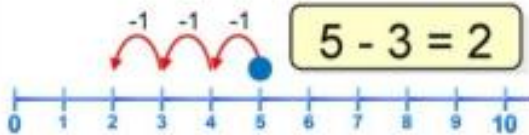
Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	 Children should have abstract supported by a pictorial or concrete if needed.
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	 Insert zeros for place holders.
Vocabulary	addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal point		

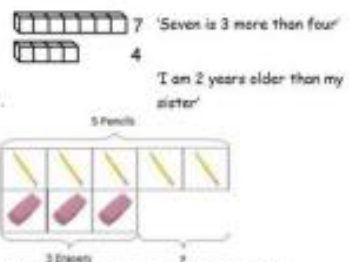
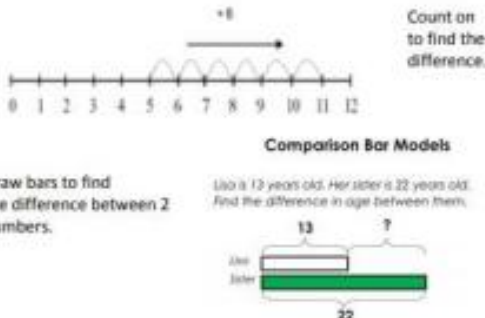
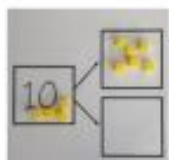
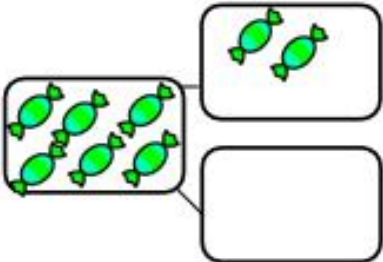
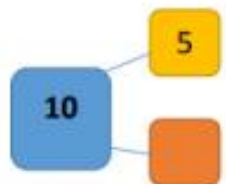
Subtraction

Subtraction- EYFS

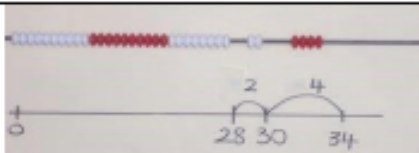
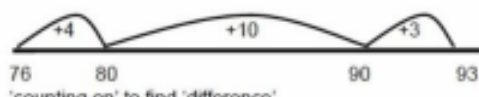
Subtraction- EYFS							
Objectives	Concrete	Pictorial	Abstract				
- Knows that a group of things change in quantity when something is taken away - Find one less from a group of five objects, then ten objects. - In practical activities and discussion, beginning to use the vocabulary involved in subtracting. - Using quantities and objects, they subtract two single digit numbers and count back to find the answer.	 Use toys and general classroom resources for children to physically manipulate, group/regroup.    Use specific maths resources such as snap cubes, Numicon, bead strings etc.  Use visual supports such as ten frames, part part whole and subtraction mats, with the physical objects and resources that can be manipulated.	  $6 - 4 =$  $3 - 1 =$  $5 - 3 =$  $7 - 2 =$ A group of pictures for children to cross out or cover quantities to support subtraction.    Use visual supports such as ten frames, part part whole and bar model with pictures/icons.	A focus on symbols and numbers to form a calculation.  $10 - 1 = ?$ $10 - 6 = 4$ <table><tr><td>3</td><td>?</td></tr><tr><td colspan="2">7</td></tr></table> $7 - 3 = ?$  * No expectation for children to be able to record a number sentence/addition calculation.	3	?	7	
3	?						
7							

Subtraction- Year 1

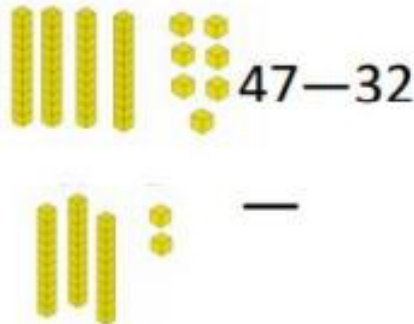
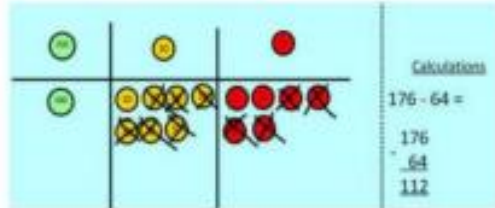
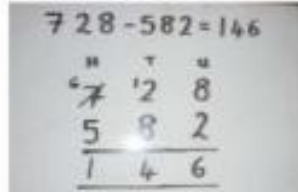
Objective and Strategy	Concrete	Pictorial	Abstract
<i>Subtract one-digit and two-digit numbers to 20, including 0.</i> Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away.  $6 - 4 = 2$ $4 - 2 = 2$	Cross out drawn objects to show what has been taken away.  $15 - 3 = 12$	$7 - 4 = 3$ $16 - 9 = 7$
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. $13 - 4$  Use counters and move them away from the group as you take them away counting backwards as you go. 	 Count back on a number line or track Start at the bigger number and count back the smaller number showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? (Use your fingers to help you)

Find the difference	Compare objects and amounts  7 'Seven is 3 more than four' 4 'I am 2 years older than my sister' 5 Pencils 3 Drawn 7 Lay objects to represent bar model.	 Count on to find the difference. Comparison Bar Models Draw bars to find the difference between 2 numbers. Use a 13 years old. Her sister is 22 years old. Find the difference in age between them.	Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?
Represent and use number bonds and related subtraction facts within 20 Part-part whole model	 Link to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the parts, what is the other part? $10 - 6 = 4$	 Use a pictorial representation of objects to show the part-part whole model	 Move to using numbers within the part whole model.
Make 10	$14 - 9 =$  Make 14 on the ten frame. Take away the four first to make 10 and then take away one more so you have taken away 5. You are left with the answer of 9.	$13 - 7 = 6$  Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	$16 - 8 =$ How many do we take off to reach the next 10? How many do we have left to take off?
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...		

Subtraction- Year 2

Objective and Strategy	Concrete	Pictorial	Abstract				
<i>Subtract a two-digit number and ones, a two-digit number and tens, two two-digit numbers</i> Partitioning to subtract without re- Grouping: 'Friendly numbers'	$34 - 13 = 21$  Use Dienes to show how to partition the number when subtracting without regrouping. The calculation will be shown alongside the manipulative used <table border="1"><thead><tr><th>Model</th><th>Calculation</th></tr></thead><tbody><tr><td></td><td></td></tr></tbody></table>	Model	Calculation			Children draw representations of Dienes and cross off.  $43 - 21 = 22$	$43 - 21 = 22$ Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: e.g. $43 - 21 = 22$ 40 and 3 <u>-20 and 1</u> <u>20 and 2</u>
Model	Calculation						
Make ten strategy	 $34 - 28$ Use a bead bar or bead strings to model counting to next ten and the rest.	 Use a number line to count on to next ten and then the rest.	$93 - 76 = 17$				
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units						

Subtraction- Year 3

Objective and Strategy	Concrete	Pictorial	Abstract				
To subtract numbers with up to three-digits, using formal written methods of columnar subtraction Column subtraction (without exchanging)	 Use base 10 or Numicon to model The calculation will be shown alongside the model chosen to see the connection <table border="1"><thead><tr><th>Model</th><th>Calculation</th></tr></thead><tbody><tr><td></td><td></td></tr></tbody></table>	Model	Calculation			Children are to be secure with use of PV counters before moving onto abstract. 	Children should begin with the expanded form. Moving onto a more formal way as below. $47-24=23$$\begin{array}{r} 40+7 \\ -20+4 \\ \hline 20+3 \end{array}$ 
Model	Calculation						

Column
Subtraction
(with
exchanging)

Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange.

Column method (using base 10 and having to exchange)

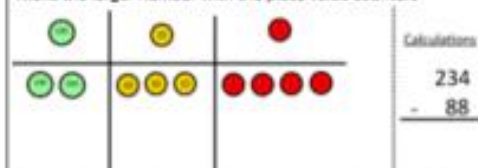
45-26



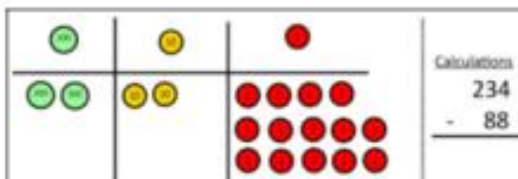
- 1) Start by partitioning 45
- 2) Exchange one ten for ten more ones
- 3) Subtract the ones, then the tens.

Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

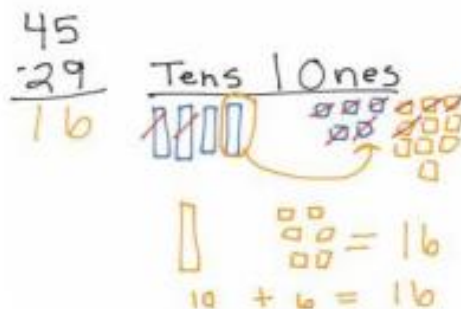
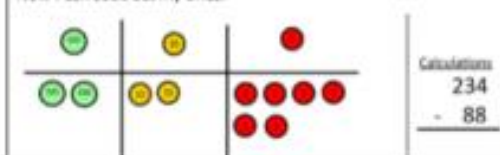
Make the larger number with the place value counters



Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Now I can subtract my ones.



When confident, children can find their own way to record the exchange/regrouping

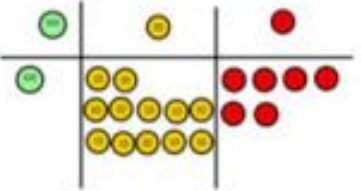
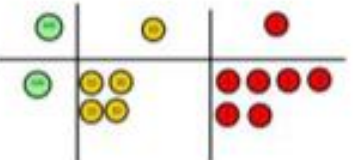
Children should begin with the expanded form. Moving onto a more formal way as below (bottom picture).

$$836 - 254 = 582$$

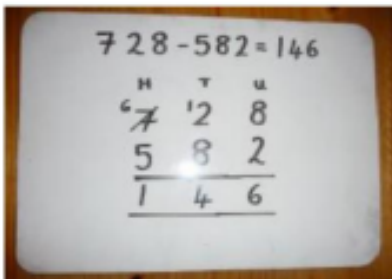
800	30	6
- 200	- 50	- 4
500	80	2

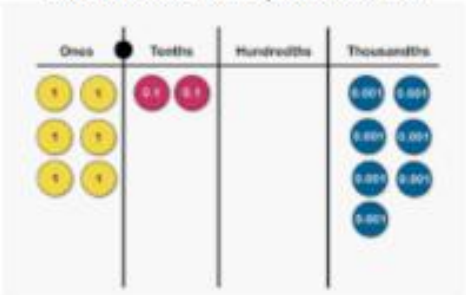
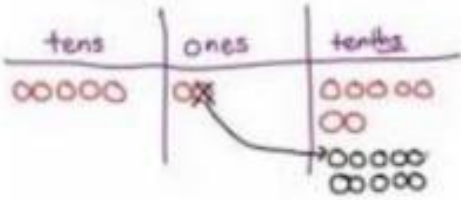
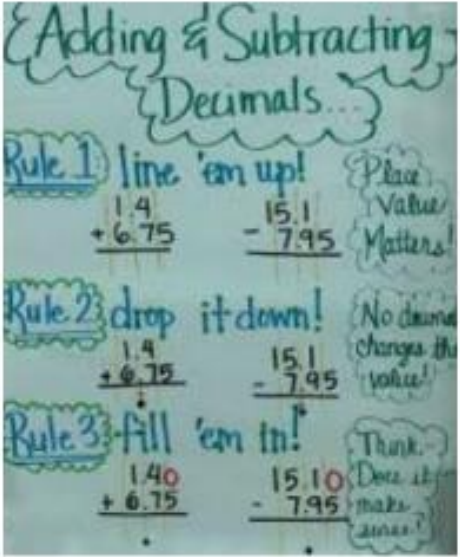
$$728 - 582 = 146$$

700	20	8
- 500	- 80	- 2
200	40	6

	Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.  Calculations $\begin{array}{r} 234 \\ - 88 \\ \hline \end{array}$ Now I can take away eight tens and complete my subtraction.  Calculations $\begin{array}{r} 234 \\ - 88 \\ \hline 146 \end{array}$ Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units

Subtraction- Year 4

Objective and Strategy	Concrete	Pictorial	Abstract								
Subtract numbers with up to 4 digits using the formal written methods appropriate of columnar subtraction where appropriate Year 4 subtractraction with up to 4 digits.	Model process of exchange using Numicon, base ten and then move to PV counters. Use the phrase 'take and make' for exchange- see Y3 The calculation will be shown alongside the model chosen to see the connection <table><tr><th>Model</th><th>Calculation</th></tr><tr><td></td><td></td></tr></table>	Model	Calculation			Children to draw pv counters and show their exchange—see Y3 The calculation will be shown alongside the model chosen to see the connection <table><tr><th>Model</th><th>Calculation</th></tr><tr><td></td><td></td></tr></table>	Model	Calculation			 This will lead to an understanding of subtracting any number including decimals.
Model	Calculation										
Model	Calculation										

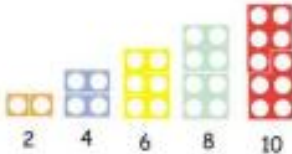
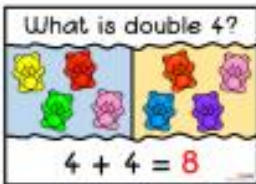
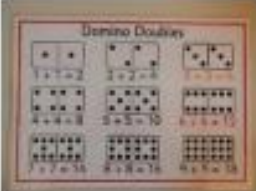
Introduce decimal subtraction through context of money	Children to be encouraged to use counters to represent numbers and take counters away to subtract. 	52.7 - 27.9  When confident, children can find their own way to record the exchange/regrouping	
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units		

Subtraction- Year 5/6

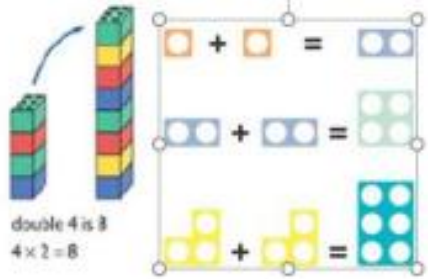
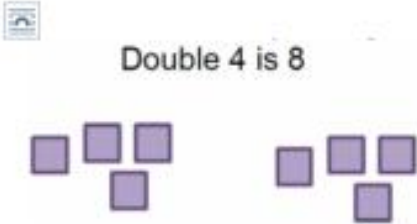
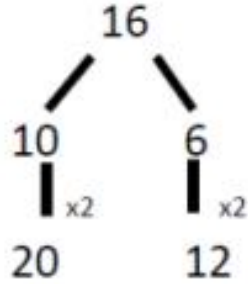
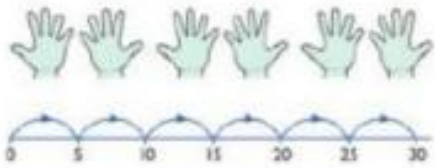
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract with at least 4 digits, including money and measures. Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).	See Year 4	See Year 4	
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units		

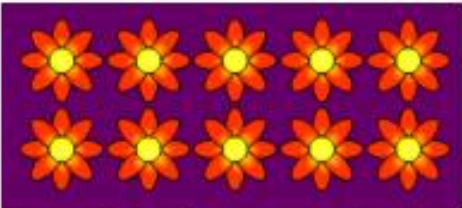
Multiplication

Multiplication-EYFS

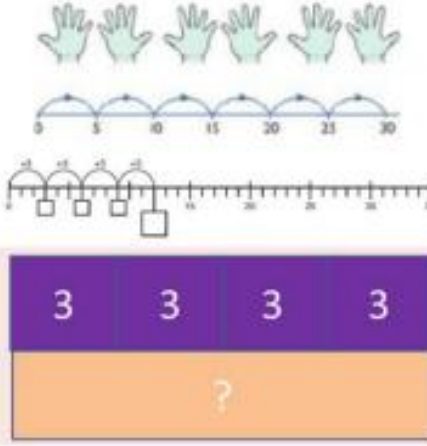
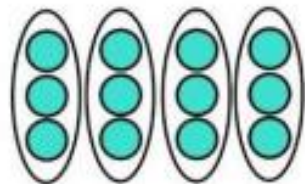
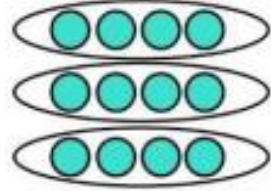
Objectives	Concrete	Pictorial	Abstract												
- Solve problems including doubling	     Counting and other maths resources for children to make 2 equal groups. Physical and real life examples that encourage children to see concept of doubling as adding two equal groups.	   Pictures and icons that encourage children to see concept of doubling as adding two equal groups.	<table><tr><td>1+1=</td><td>7+7=</td></tr><tr><td>2+2=</td><td>8+8=</td></tr><tr><td>3+3=</td><td>9+9=</td></tr><tr><td>4+4=</td><td>10+10=</td></tr><tr><td>5+5=</td><td>11+11=</td></tr><tr><td>6+6=</td><td>12+12=</td></tr></table> Addition calculations to model adding two equal groups.	1+1=	7+7=	2+2=	8+8=	3+3=	9+9=	4+4=	10+10=	5+5=	11+11=	6+6=	12+12=
1+1=	7+7=														
2+2=	8+8=														
3+3=	9+9=														
4+4=	10+10=														
5+5=	11+11=														
6+6=	12+12=														

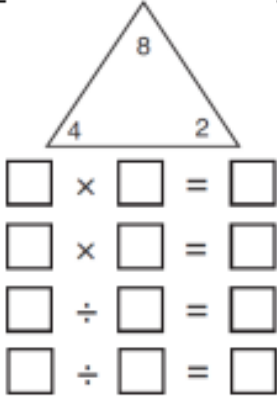
Multiplication- Year 1

Objective and Strategy	Concrete	Pictorial	Abstract
Doubling	Use practical activities using <u>manipulatives</u> including cubes and Numicon to demonstrate doubling 	Draw pictures to show how to double numbers 	Partition a number and then double each part before recombining it back together. 
Counting in multiples	 Count in multiples supported by concrete objects in equal groups.	 Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Repeated addition	 Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 	Write addition sentences to describe objects and pictures. 

		Use pictorial including number lines to solve problems. There are 3 sweets in one bag. How many sweets are in 5 bags altogether?  $3+3+3+3+3 = 15$ 	
Understanding arrays	Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc. 		$3 \times 2 = 6$ $2 \times 5 = 10$
Vocabulary	Groups of, lots of, times, array, altogether, multiply		

Multiplication- Year 2

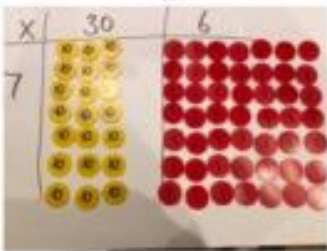
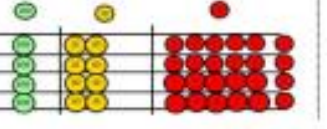
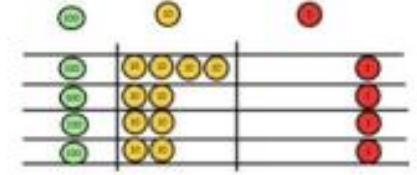
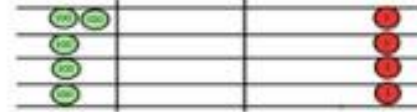
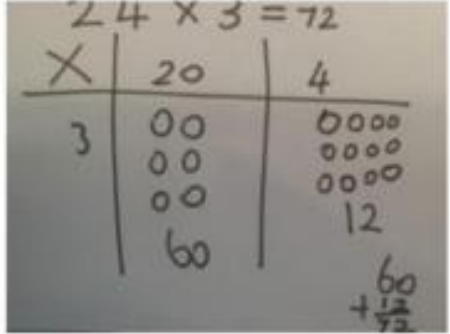
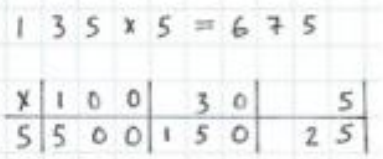
Objective and Strategy	Concrete	Pictorial	Abstract
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models.  $5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$ 	Number lines, counting sticks and bar models should be used to show <u>representation</u> of counting in multiples. 	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30 $4 \times 3 = \square$
Multiplication is commutative	Create arrays using counters and cubes and Numicon.    Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.  	Use representations of arrays to show different calculations and explore commutativity.  	$12 = 3 \times 4$ $12 = 4 \times 3$ Use an array to write multiplication sentences and reinforce repeated addition.  $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$

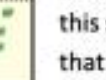
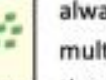
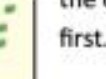
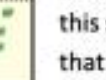
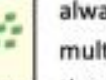
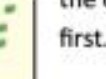
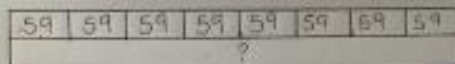
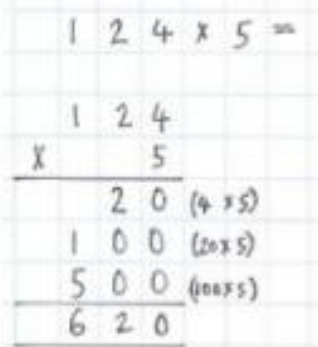
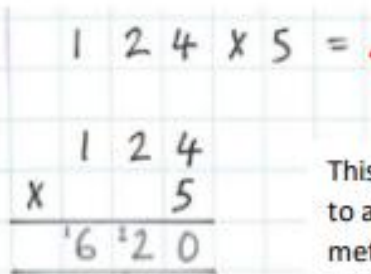
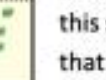
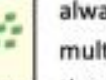
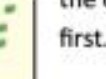
Using the Inverse <i>This should be taught alongside division, so pupils learn how they work alongside each other.</i>		 $\begin{array}{l} \square \times \square = \square \\ \square \times \square = \square \\ \square \div \square = \square \\ \square \div \square = \square \end{array}$	2 x 4 = 8 4 x 2 = 8 8 + 2 = 4 8 + 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 + 4 4 = 8 + 2 Show all 8 related fact family sentences.
Vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative.		

Multiplication- Year 3

Objective and Strategy	Concrete	Pictorial	Abstract																						
<i>Multiplying two digit number by a one digit number</i> Grid method progressing to the formal method. Solving problems including missing number problems, integer scaling problems.	Show the link with arrays to first introduce the grid method. <table><tr><td>x</td><td>10</td><td>3</td></tr><tr><td>4</td><td></td><td></td></tr></table> 4 rows of 10 4 rows of 3 Move on to using Base 10 to move towards a more compact method. <table><tr><td>x</td><td>T</td><td>U</td></tr><tr><td></td><td></td><td></td></tr></table> 4 rows of 13 Move on to place value counters to show how we are finding groups of a number. <table><tr><td>x</td><td>30</td><td>6</td></tr><tr><td>7</td><td></td><td></td></tr></table> Add up each column, starting with the ones making any exchanges needed. The calculation will be shown alongside the model chosen to see the connection <table><tr><th>Model</th><th>Calculation</th></tr><tr><td></td><td></td></tr></table>	x	10	3	4			x	T	U				x	30	6	7			Model	Calculation			Children can represent their work with place value counters in a way that they understand. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below. Bar model are used to explore missing numbers	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. TO x O Children to add up each column to find the answer.
x	10	3																							
4																									
x	T	U																							
x	30	6																							
7																									
Model	Calculation																								
Vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up																								

Multiplication- Year 4

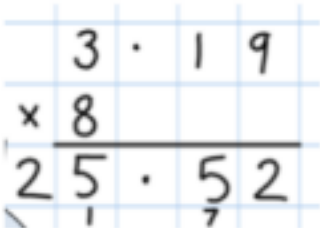
Objective and Strategy	Concrete	Pictorial	Abstract
<i>Multiply two-digit and three-digit numbers by a one-digit number using formal written layout</i> Grid method recap from year 3 for 2 digits x 1 digit Multiplying numbers by 1 digit (year 4 expectation)	 Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.  Calculations 4 x 126 Fill each row with 126.  Calculations 4 x 126 Add up each column, starting with the ones making any exchanges needed.  Then you have your answer. 	Children can represent their work with place value counters in a way that they understand. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below. 	HTO x O  Children to add up each column to find the answer.

Column multiplication	Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2 = 642$ <table border="1"><thead><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr></thead><tbody><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></tbody></table> It is important at this stage that they always multiply the ones first. The corresponding long multiplication is modelled alongside <table border="1"><thead><tr><th>Model</th><th>Calculation</th></tr></thead><tbody><tr><td></td><td></td></tr></tbody></table>	Hundreds	Tens	Ones													Model	Calculation			This grid method may be used to show how this relates to a formal written method. <table border="1"><thead><tr><th>x</th><th>100</th><th>20</th><th>4</th></tr></thead><tbody><tr><th>5</th><td>500</td><td>100</td><td>20</td></tr></tbody></table>  $= 8 \times 59$ $8 \times 60 - 8$ $8 \times 6 = 48$ $8 \times 60 = 480$ $480 - 8 = 472$ Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.	x	100	20	4	5	500	100	20	  This may lead to a compact method.
Hundreds	Tens	Ones																												
																														
																														
																														
																														
Model	Calculation																													
x	100	20	4																											
5	500	100	20																											
Vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive																													

Multiplication Year 5

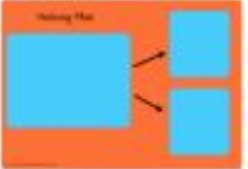
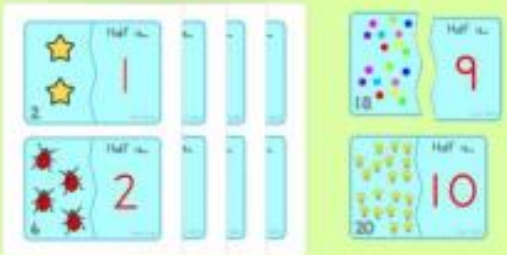
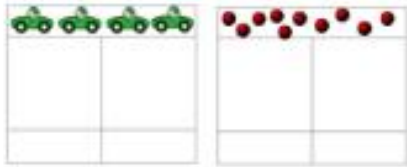
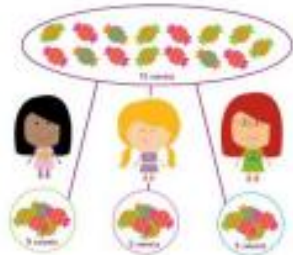
Objective and Strategy	Concrete	Pictorial	Abstract																															
Multiply numbers up to 4-digits by a one-digit number using the format written method, including long multiplication for 2-digit numbers Column multiplication for 3 and 4 digits x 1 digit	Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2 = 642$ <table><tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td></tr></table> It is important at this stage that they always multiply the ones first. The corresponding long multiplication is modelled alongside	Hundreds	Tens	Ones													<table><tr><td>x</td><td>300</td><td>20</td><td>7</td></tr><tr><td>4</td><td>1200</td><td>80</td><td>28</td></tr></table>	x	300	20	7	4	1200	80	28	$\begin{array}{r} 327 \\ \times 4 \\ \hline 28 \\ 80 \\ 1200 \\ \hline 1308 \end{array}$ $\begin{array}{r} 327 \\ \times 4 \\ \hline 1308 \\ \text{1 2} \end{array}$ This may lead to a compact method.								
Hundreds	Tens	Ones																																
x	300	20	7																															
4	1200	80	28																															
Column multiplication (long multiplication)	Manipulatives may still be used with the corresponding long multiplication modelled alongside <table><tr><th>Model</th><th>Calculation</th></tr><tr><td></td><td></td></tr></table>	Model	Calculation			Moving forward, multiply by a 2 digit number showing the different rows within the grid method. <table><tr><td>2</td><td>4</td><td>x</td><td>1</td><td>6</td><td>=</td><td>3</td><td>8</td><td>4</td></tr><tr><td>1</td><td>0</td><td>2</td><td>0</td><td>0</td><td></td><td>4</td><td>0</td><td></td></tr><tr><td>6</td><td>1</td><td>2</td><td>0</td><td></td><td></td><td>2</td><td>4</td><td></td></tr></table>	2	4	x	1	6	=	3	8	4	1	0	2	0	0		4	0		6	1	2	0			2	4		$\begin{array}{r} 24 \\ \times 16 \\ \hline 144 \\ 240 \\ \hline 384 \end{array}$ 24 x 6 on the first row. (6 x 4 = 24, carrying the 2 for the 20, then 6 x 2) 24 x 10 on the second row. Show multiplying by 10 by putting zero in the units first. $\begin{array}{r} 1234 \\ \times 16 \\ \hline 7404 \\ 12340 \\ \hline 19744 \end{array}$ (1234 x 6) (1234 x 10)
Model	Calculation																																	
2	4	x	1	6	=	3	8	4																										
1	0	2	0	0		4	0																											
6	1	2	0			2	4																											
Vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive, factor pairs, composite numbers, prime number, factors, squared, cubed																																	

Multiplication- Year 6

Objective and Strategy	Concrete	Pictorial	Abstract
Multiply decimal up to 2 decimal place by a single digit.			Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer. 
vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive, factor pairs, composite numbers, prime number, factors, squared, cubed		

Division

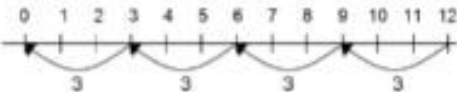
Division- EYFS

Objectives	Concrete	Pictorial	Abstract
Solve problems including halving and sharing. - Halving a whole, halving a quantity of objects. - Sharing a quantity of objects.	  Children have the opportunity to physically cut objects, food or shapes in half.  Counting and other maths resources for children to share into two equal groups.   Use visual supports such as halving mats and part part whole, with the physical objects and resources that can be manipulated.  Counting and other maths resources for children to explore sharing between 3 or more.	 Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. i.e. Knowing 4 is made of 2 groups of 2, so half of 4 is 2.  Bar model with pictures or icons to support understanding of finding 2 equal parts of a number, to further understand how two halves make a whole.  Pictures for children to create and visualise 3 or more equal groups.	

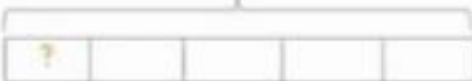
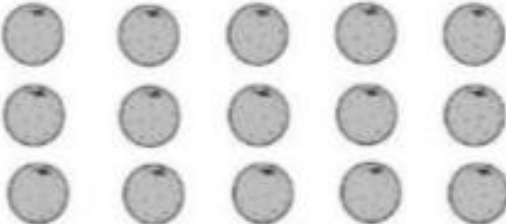
Division- Year 1

Objective and Strategy	Concrete	Pictorial	Abstract
Division as sharing (sharing objects into groups)	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$ Children use bar modelling to show and support understanding. $12 \div 4 = 3$	Share 9 buns between three people. $9 \div 3 = 3$
Vocabulary	share, share equally, one each, two each..., group, groups of, lots of, array		

Division- Year 2

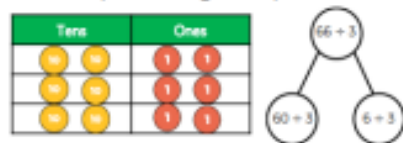
Objective and Strategy	Concrete	Pictorial	Abstract
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.  $96 \div 3 = 32$   	Use a number line to show jumps in groups. The number of jumps equals the number of groups.  Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group. 	$28 \div 7 = 4$ Divide 28 into 7 groups. How many are in each group?
Vocabulary	share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over		

Division- Year 3

Objective and Strategy	Concrete	Pictorial	Abstract
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding.  24 divided into groups of 6 = 4 $96 \div 3 = 32$ 	Continue to use bar modelling to aid solving division problems.  $20 \div 5 = ?$ $5 \times ? = 20$	How many groups of 6 in 24? $24 \div 6 = 4$
Division with arrays	 Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array and use lines to split the array into groups to make multiplication and division sentences 	Find the inverse of multiplication and division sentences by creating eight linking number sentences. $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$ $28 = 7 \times 4$ $28 = 4 \times 7$ $4 = 28 \div 7$ $7 = 28 \div 4$

Divide 2-digit numbers by a 1-digit number by partitioning into tens and ones using a pv grid

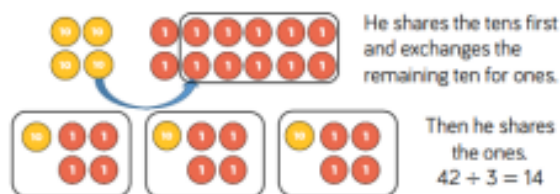
Eva uses a place value grid and part-whole model to solve $66 \div 3$



See part-whole model

Divide numbers that involve exchanging between the tens and ones. The answers do not have remainders.

Ron uses place value counters to divide 42 into three equal groups.



Annie uses a similar method to divide 42 by 3



Children may use pictorial representation for the pv counters, alongside the part-whole model

Children use their times-tables to partition the number into multiples of the divisor.

$$\begin{array}{l} 96 \div 8 \\ 96 \div 4 \\ 96 \div 3 \\ 96 \div 6 \end{array}$$

Compare the statements using $<$, $>$ or $=$

$$48 \div 4 \bigcirc 36 \div 3$$

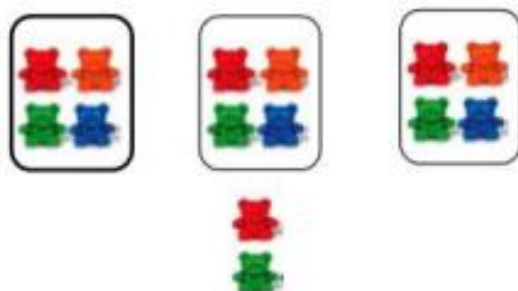
$$52 \div 4 \bigcirc 42 \div 3$$

$$60 \div 3 \bigcirc 60 \div 4$$

Division with a remainder

$$14 \div 3 =$$

Divide objects between groups and see how much is left over



Moving on to:

- Use place value counters to work out $94 \div 4$
- Did you need to exchange any tens for ones?
- Is there a remainder?



29

Tens	Ones

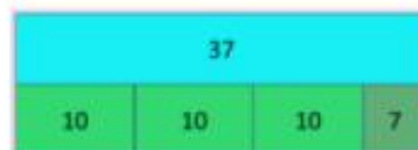
Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



Draw dots and group them to divide an amount and clearly show a remainder.



Use bar models to show division with remainders.



Complete written divisions and show the remainder using r.

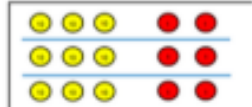
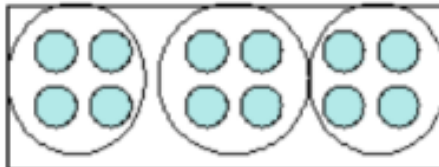
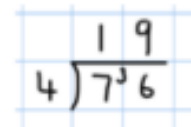
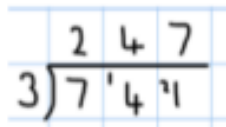
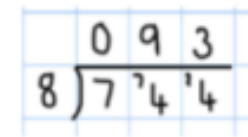
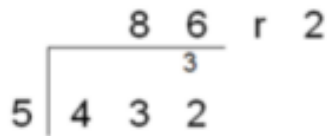
$$29 \div 8 = 3 \text{ REMAINDER } 5$$

↑ ↑ ↑ ↑
dividend divisor quotient remainder

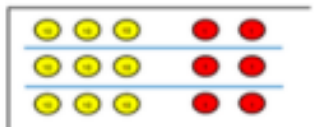
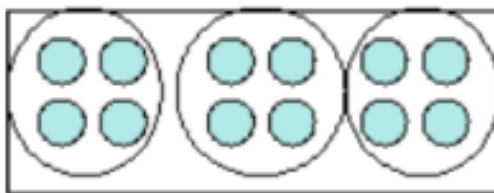
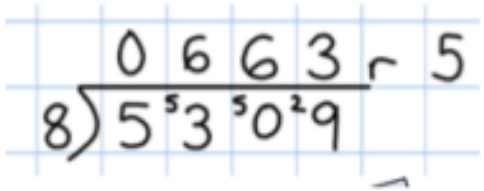
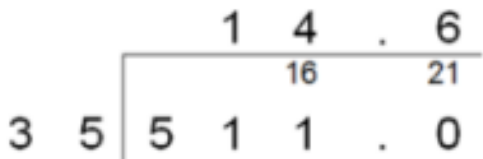
Vocabulary

share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product

Division- Year 4

Objective and Strategy	Concrete	Pictorial	Abstract
Divide up to 3 digit numbers by 1 digit. Short Division	$96 \div 3$ Tens Units 3 2  Use place value counters to divide using the bus stop method alongside  $42 \div 3 =$ Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.  We exchange this ten for ten ones and then share the ones equally among the groups.  We look how much in 1 group so the answer is 14.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.  Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder   Children should be aware that a 0 is used to keep place value, if the number is not divisible.  Move onto divisions with a remainder. 
Vocabulary	share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive		

Division- Year 5

Objective and Strategy	Concrete	Pictorial	Abstract
<i>Divide at least 4 digit numbers by 1 digit. Interpret remainders appropriately for the context</i> Short Division	$96 \div 3$ Tens Units 3 2  Use place value counters to divide using the bus stop method alongside  42 $\div$ 3 = Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.  We exchange this ten for ten ones and then share the ones equally among the groups.  We look how much in 1 group so the answer is 14.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.  Encourage them to move towards counting in multiples to divide more efficiently.	 Finally move into decimal places to divide the total accurately. 
Vocabulary	share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.		

Division-Year 6

Objective and Strategy

Abstract

Long Division

Step 1 – a remainder in the ones

$$\begin{array}{r} \text{h t o} \\ 041 \text{ R1} \\ 4 \overline{) 165} \end{array}$$

4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).

4 goes into 16 four times.

4 goes into 5 once, leaving a remainder of 1.

$$\begin{array}{r} \text{th h t o} \\ 0400 \text{ R7} \\ 8 \overline{) 3207} \end{array}$$

8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).

8 goes into 32 four times ($3,200 \div 8 = 400$)

8 goes into 0 zero times (tens).

8 goes into 7 zero times, and leaves a remainder of 7.

$$\begin{array}{r} \text{h t o} \\ 061 \\ 4 \overline{) 247} \\ \underline{-4} \\ 3 \end{array}$$

When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$, write that four under the 7, and subtract. This finds us the remainder of 3.

Check: $4 \times 61 + 3 = 247$

$$\begin{array}{r} \text{th h t o} \\ 0402 \\ 4 \overline{) 1609} \\ \underline{-8} \\ 1 \end{array}$$

When dividing the ones, 4 goes into 9 two times. Multiply $2 \times 4 = 8$, write that eight under the 9, and subtract. This finds us the remainder of 1.

Check: $4 \times 402 + 1 = 1,609$

Step 2 – a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \end{array}$ Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens -- but there is a remainder!	$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ -4 \\ \hline 1 \end{array}$ To find it, multiply $2 \times 2 = 4$, write that 4 under the five, and subtract to find the remainder of 1 ten.	$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ -4 \\ \hline 18 \end{array}$ Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ -4 \\ \hline 18 \end{array}$ Divide 2 into 18. Place 9 into the quotient.	$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ -4 \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ Multiply $9 \times 2 = 18$, write that 18 under the 18, and subtract.	$\begin{array}{r} \text{t o} \\ 2 \overline{) 58} \\ -4 \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ The division is over since there are no more digits in the dividend. The quotient is 29.

Step 3 – a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{h t o} \\ 1 \\ 2 \overline{) 278} \end{array}$ Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	$\begin{array}{r} \text{h t o} \\ 1 \\ 2 \overline{) 278} \\ \underline{2} \\ 0 \end{array}$ Multiply $1 \times 2 = 2$, write that 2 under the two, and subtract to find the remainder of zero.	$\begin{array}{r} \text{h t o} \\ 18 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \end{array}$ Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \end{array}$ Divide 2 into 7. Place 3 into the quotient.	$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \\ \underline{-6} \\ 1 \end{array}$ Multiply $3 \times 2 = 6$, write that 6 under the 7, and subtract to find the remainder of 1 ten.	$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \\ \underline{-6} \\ 18 \end{array}$ Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \\ \underline{-6} \\ 18 \end{array}$ Divide 2 into 18. Place 9 into the quotient.	$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \\ \underline{-6} \\ 18 \\ \underline{-18} \\ 0 \end{array}$ Multiply $9 \times 2 = 18$, write that 18 under the 18, and subtract to find the remainder of zero.	$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{) 278} \\ \underline{-2} \\ 07 \\ \underline{-6} \\ 18 \\ \underline{-18} \\ 0 \end{array}$ There are no more digits to drop down. The quotient is 139.

Vocabulary

share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.